Coprime Mappings and Lonely Runners

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Time: Dec 20th, 14:00 - 15:00
Zoom meeting ID: 898 1138 0689  Password: 121323
Link: https://zoom.us/j/89811380689

Abstract:

The lonely runner conjecture can be stated as follows: for any $n$ positive integers $v_1 < v_2 < \ldots < v_n$ there exists a real number $t$ such that each $v_it$ is at least $1/(n + 1)$ away from the nearest integer. In this paper we prove that this is true if $v_n < (2 - \varepsilon)n$. This is an approximate version of a natural next step for the study of the lonely runner conjecture suggested by Tao.

The key ingredient in our proof is a result on coprime mappings. Let $A$ and $B$ be sets of integers. A bijection $f : A \rightarrow B$ is a coprime mapping if $a$ and $f(a)$ are coprime for every $a \in A$. We show that if $A, B \subset [n]$ are intervals of length $2m$ where $m = \exp(\Omega((\log \log n)^2))$ then there exists a coprime mapping from $A$ to $B$. This is based on joint work with Tom Bohman.